

```

//*****
//      Matrix Chain Order
//*****
Matrix-Chain-Order(p)
  n = length[p] - 1 // n is the number of matrix multiplies needed
  // Initialize results array
  for i = 1 to n
    do m[i,i] = 0
  for l = 2 to n // l is the diagonal to fill in
    do for i = 1 to n - l + 1 // work down the diagonal; i is the row;
      do j = i + l - 1 // column j depends on diagonal and row
        m[i,j] = INFINITY // initialize result so we can find min
        for k = i to j - 1 // check all possible split points k
          do q = m[i,k] + m[k+1,j] + p[i-1]*p[k]*p[j]
            if q < m[i,j]
              then m[i,j] = q
                s[i,j] = k // save split point so
                  // multiplication order can be
                  // reconstructed

return m and s

```

## Memoized-Matrix-Chain(p)

```
// Initialize results array and call auxilliary recursive function
n = length[p] - 1 // n is the number of matrix multiplies needed
for i = 1 to n
    do for j = i to n
        do m[i,i] = INFINITY
return Lookup-Chain(p, 1, n)
```

## Lookup-Chain(p, i, j)

```
if m[i,j] < INFINITY
    then return m[i,j]
if i == j
    then m[i,j] = 0
else for k = i to j - 1 // check all possible split points k
    do q = Lookup-Chain(p,i,k) + Lookup-Chain(k+1,j)
        + p[i-1]*p[k]*p[j]
        if q < m[i,j]
            then m[i,j] = q
return m[i,j]
```