Problem H

Consider a tennis racket to be a flat, two-dimensional shape. The normal to the plane of the racket is a principal direction, which we will take to be $\hat{e}_1$. The direction along the handle is another principal direction, which we take to be $\hat{e}_2$, and finally, the direction in the plane of the racket perpendicular to the handle is $\hat{e}_3$.

(a) Make a sketch showing these principal directions on the racket, with the origin at the center of mass.

(b) For a real tennis racket, the moment of inertia values are typically $\lambda_1 = 1.5 \times 10^{-3}$ kg·m$^2$, $\lambda_2 = 36.5 \times 10^{-3}$ kg·m$^2$, and $\lambda_3 = 35.0 \times 10^{-2}$ kg·m$^2$. Consider flipping the racket about the $\hat{e}_3$ axis, rotating it with frequency $\omega_3$. The initial rotation will typically include some tiny amount of non-zero $\omega_1$ and $\omega_2$ as well.

By what factor will the initial $\omega_1$ value increase in the time it takes for the racket to complete one oscillation about the $\hat{e}_3$ axis? Comment on your result.