

Text Clustering

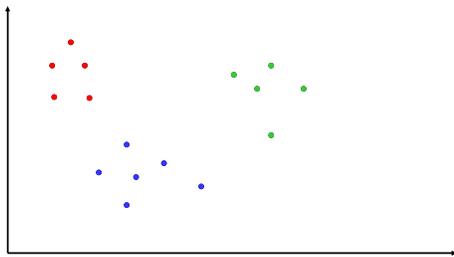
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Clustering

- Partition unlabeled examples into disjoint subsets of *clusters*, such that:
 - Examples within a cluster are very similar
 - Examples in different clusters are very different
- Discover new categories in an *unsupervised* manner (no sample category labels provided).

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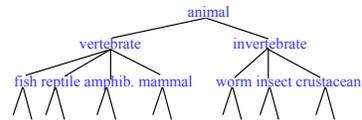
Clustering Example



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Hierarchical Clustering

- Build a tree-based hierarchical taxonomy (*dendrogram*) from a set of unlabeled examples.



- Recursive application of a standard clustering algorithm can produce a hierarchical clustering.

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Agglomerative vs. Divisive Clustering

- *Agglomerative* (*bottom-up*) methods start with each example in its own cluster and iteratively combine them to form larger and larger clusters.
- *Divisive* (*partitional, top-down*) separate all examples immediately into clusters.

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Direct Clustering Method

- *Direct clustering* methods require a specification of the number of clusters, k , desired.
- A *clustering evaluation function* assigns a real-value quality measure to a clustering.
- The number of clusters can be determined automatically by explicitly generating clusterings for multiple values of k and choosing the best result according to a clustering evaluation function.

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Hierarchical Agglomerative Clustering (HAC)

- Assumes a *similarity function* for determining the similarity of two instances.
- Starts with all instances in a separate cluster and then repeatedly joins the two clusters that are most similar until there is only one cluster.
- The history of merging forms a binary tree or hierarchy.

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HAC Algorithm

Start with all instances in their own cluster.

Until there is only one cluster:

Among the current clusters, determine the two clusters, c_i and c_j , that are most similar.

Replace c_i and c_j with a single cluster $c_i \cup c_j$

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Cluster Similarity

- Assume a similarity function that determines the similarity of two instances: $sim(x, y)$.
 - Cosine similarity of document vectors.
- How to compute similarity of two clusters each possibly containing multiple instances?
 - **Single Link**: Similarity of two most similar members.
 - **Complete Link**: Similarity of two least similar members.
 - **Group Average**: Average similarity between members.

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Single Link Agglomerative Clustering

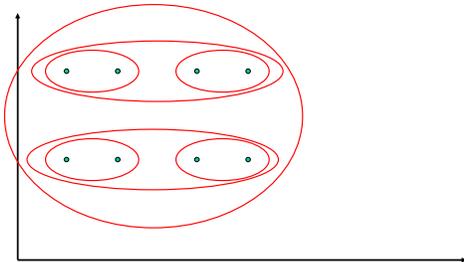
- Use maximum similarity of pairs:

$$sim(c_i, c_j) = \max_{x \in c_i, y \in c_j} sim(x, y)$$

- Can result in “straggly” (long and thin) clusters due to *chaining effect*.
 - Appropriate in some domains, such as clustering islands.

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Single Link Example



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Complete Link Agglomerative Clustering

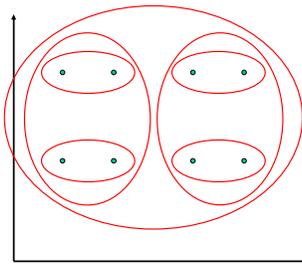
- Use minimum similarity of pairs:

$$sim(c_i, c_j) = \min_{x \in c_i, y \in c_j} sim(x, y)$$

- Makes more “tight,” spherical clusters that are typically preferable.

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Complete Link Example



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Computational Complexity

- In the first iteration, all HAC methods need to compute similarity of all pairs of n individual instances which is $O(n^2)$.
- In each of the subsequent $n-2$ merging iterations, it must compute the distance between the most recently created cluster and all other existing clusters.
- In order to maintain an overall $O(n^2)$ performance, computing similarity to each other cluster must be done in constant time.

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Computing Cluster Similarity

- After merging c_i and c_j , the similarity of the resulting cluster to any other cluster, c_k , can be computed by:
 - Single Link:

$$\text{sim}((c_i \cup c_j), c_k) = \max(\text{sim}(c_i, c_k), \text{sim}(c_j, c_k))$$
 - Complete Link:

$$\text{sim}((c_i \cup c_j), c_k) = \min(\text{sim}(c_i, c_k), \text{sim}(c_j, c_k))$$

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Group Average Agglomerative Clustering

- Use average similarity across all pairs within the merged cluster to measure the similarity of two clusters.

$$\text{sim}(c_i, c_j) = \frac{1}{|c_i \cup c_j|(|c_i \cup c_j| - 1)} \sum_{\bar{x} \in (c_i \cup c_j)} \sum_{\bar{y} \in (c_i \cup c_j), \bar{y} \neq \bar{x}} \text{sim}(\bar{x}, \bar{y})$$
- Compromise between single and complete link.
- Averaged across all ordered pairs in the merged cluster instead of unordered pairs *between* the two clusters.

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Computing Group Average Similarity

- Assume cosine similarity and normalized vectors with unit length.
- Always maintain sum of vectors in each cluster.

$$\bar{s}(c_j) = \sum_{\bar{x} \in c_j} \bar{x}$$
- Compute similarity of clusters in constant time:

$$\text{sim}(c_i, c_j) = \frac{(\bar{s}(c_i) + \bar{s}(c_j)) \bullet (\bar{s}(c_i) + \bar{s}(c_j)) - (|c_i| + |c_j|)}{(|c_i| + |c_j|)(|c_i| + |c_j| - 1)}$$

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Non-Hierarchical Clustering

- Typically must provide the number of desired clusters, k .
- Randomly choose k instances as *seeds*, one per cluster.
- Form initial clusters based on these seeds.
- Iterate, repeatedly reallocating instances to different clusters to improve the overall clustering.
- Stop when clustering converges or after a fixed number of iterations.

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K-Means

- Assumes instances are real-valued vectors.
- Clusters based on *centroids*, *center of gravity*, or mean of points in a cluster, c :

$$\bar{\mu}(c) = \frac{1}{|c|} \sum_{\bar{x} \in c} \bar{x}$$

- Reassignment of instances to clusters is based on distance to the current cluster centroids.

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Distance Metrics

- Euclidian distance (L_2 norm):

$$L_2(\bar{x}, \bar{y}) = \sum_{i=1}^m (x_i - y_i)^2$$

- L_1 norm:

$$L_1(\bar{x}, \bar{y}) = \sum_{i=1}^m |x_i - y_i|$$

- Cosine Similarity (transform to a distance by subtracting from 1):

$$1 - \frac{\bar{x} \cdot \bar{y}}{|\bar{x}| \cdot |\bar{y}|}$$

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K-Means Algorithm

Let d be the distance measure between instances.

Select k random instances $\{s_1, s_2, \dots, s_k\}$ as seeds.

Until clustering converges or other stopping criterion:

For each instance x_i :

Assign x_i to the cluster c_j such that $d(x_i, s_j)$ is minimal.

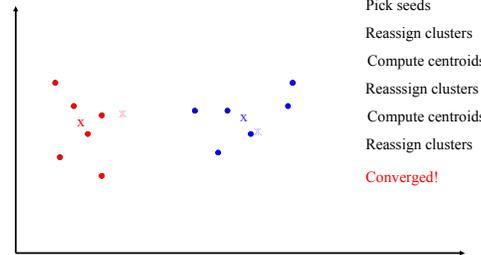
(Update the seeds to the centroid of each cluster)

For each cluster c_j

$$s_j = \mu(c_j)$$

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K Means Example (K=2)



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Time Complexity

- Assume computing distance between two instances is $O(m)$ where m is the dimensionality of the vectors.
- Reassigning clusters: $O(kn)$ distance computations, or $O(knm)$.
- Computing centroids: Each instance vector gets added once to some centroid: $O(nm)$.
- Assume these two steps are each done once for I iterations: $O(Iknm)$.
- Linear in all relevant factors, assuming a fixed number of iterations, more efficient than $O(n^2)$ HAC.

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Seed Choice

- Results can vary based on random seed selection.
- Some seeds can result in poor convergence rate, or convergence to sub-optimal clusterings.
- Select good seeds using a heuristic or the results of another method.

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Buckshot Algorithm

- Combines HAC and K-Means clustering.
- First randomly take a sample of instances of size \sqrt{n}
- Run group-average HAC on this sample, which takes only $O(n)$ time.
- Use the results of HAC as initial seeds for K-means.
- Overall algorithm is $O(n)$ and avoids problems of bad seed selection.

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Text Clustering

- HAC and K-Means have been applied to text in a straightforward way.
- Typically use **normalized**, TF/IDF-weighted vectors and cosine similarity.
- Optimize computations for sparse vectors.
- Applications:
 - During retrieval, add other documents in the same cluster as the initial retrieved documents to improve recall.
 - Clustering of results of retrieval to present more organized results to the user (à la Northernlight folders).
 - Automated production of hierarchical taxonomies of documents for browsing purposes (à la Yahoo & DMOZ).

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Soft Clustering

- Clustering typically assumes that each instance is given a “hard” assignment to exactly one cluster.
- Does not allow uncertainty in class membership or for an instance to belong to more than one cluster.
- **Soft clustering** gives probabilities that an instance belongs to each of a set of clusters.
- Each instance is assigned a probability distribution across a set of discovered categories (probabilities of all categories must sum to 1).

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Expectation Maximization (EM)

- Probabilistic method for soft clustering.
- Direct method that assumes k clusters: $\{c_1, c_2, \dots, c_k\}$
- Soft version of k -means.
- Assumes a probabilistic model of categories that allows computing $P(c_i | E)$ for each category, c_i , for a given example, E .
- For text, typically assume a naïve-Bayes category model.
 - Parameters $\theta = \{P(c_j), P(w_j | c_j): i \in \{1, \dots, k\}, j \in \{1, \dots, |V|\}\}$

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EM Algorithm

- Iterative method for learning probabilistic categorization model from unsupervised data.
- Initially assume random assignment of examples to categories.
- Learn an initial probabilistic model by estimating model parameters θ from this randomly labeled data.
- Iterate following two steps until convergence:
 - **Expectation (E-step)**: Compute $P(c_i | E)$ for each example given the current model, and probabilistically re-label the examples based on these posterior probability estimates.
 - **Maximization (M-step)**: Re-estimate the model parameters, θ , from the probabilistically re-labeled data.

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Learning from Probabilistically Labeled Data

- Instead of training data labeled with “hard” category labels, training data is labeled with “soft” probabilistic category labels.
- When estimating model parameters θ from training data, weight counts by the corresponding probability of the given category label.
- For example, if $P(c_1 | E) = 0.8$ and $P(c_2 | E) = 0.2$, each word w_j in E contributes only 0.8 towards the counts n_1 and n_{1j} , and 0.2 towards the counts n_2 and n_{2j} .

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Naïve Bayes EM

Randomly assign examples probabilistic category labels.
Use standard naïve-Bayes training to learn a probabilistic model with parameters θ from the labeled data.
Until convergence or until maximum number of iterations reached:
E-Step: Use the naïve Bayes model θ to compute $P(c_i | E)$ for each category and example, and re-label each example using these probability values as soft category labels.
M-Step: Use standard naïve-Bayes training to re-estimate the parameters θ using these new probabilistic category labels.

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Semi-Supervised Learning

- For supervised categorization, generating labeled training data is expensive.
- **Idea:** Use unlabeled data to aid supervised categorization.
- Use EM in a *semi-supervised* mode by training EM on both labeled and unlabeled data.
 - Train initial probabilistic model on user-labeled subset of data instead of randomly labeled unsupervised data.
 - Labels of user-labeled examples are “frozen” and never relabeled during EM iterations.
 - Labels of unsupervised data are constantly probabilistically relabeled by EM.

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Semi-Supervised Example

- Assume “quantum” is present in several labeled physics documents, but “Heisenberg” occurs in *none* of the *labeled* data.
- From labeled data, learn that “quantum” is indicative of a physics document.
- When labeling unsupervised data, label several documents with “quantum” *and* “Heisenberg” correctly with the “physics” category.
- When retraining, learn that “Heisenberg” is also indicative of a physics document.
- Final learned model is able to correctly assign documents containing *only* “Heisenberg” to physics.

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Semi-Supervision Results

- Experiments on assigning messages from 20 Usenet newsgroups their proper newsgroup label.
- With very few labeled examples (2 examples per class), semi-supervised EM improved accuracy from 27% (supervised data only) to 43% (supervised + unsupervised data).
- With more labeled examples, semi-supervision can actually decrease accuracy, but refinements to standard EM can prevent this.
- For semi-supervised EM to work, the “natural clustering of data” must be consistent with the desired categories.

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