

\*\*\*\*\*9-CAGE-15\*\*\*\*\*

Edges of 9-CAGE-15:

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( 9 10) ( 18 19) ( 40 41) ( 37 38) ( 14 15) ( 21 30)
( 40 56) ( 3 4) ( 15 23) ( 39 40) ( 24 43) ( 26 27)
( 7 8) ( 52 53) ( 12 27) ( 16 17) ( 57 58) ( 31 47)
( 50 51) ( 17 18) ( 1 2) ( 8 9) ( 46 47) ( 54 55)
( 51 52) ( 29 30) ( 29 37) ( 19 20) ( 26 57) ( 32 33)
( 7 54) ( 27 28) ( 22 23) ( 36 44) ( 43 44) ( 10 42)
( 33 34) ( 18 34) ( 56 57) ( 49 50) ( 5 17) ( 32 41)
( 47 48) ( 41 42) ( 24 25) ( 16 39) ( 20 55) ( 33 52)
( 36 37) ( 44 45) ( 2 22) ( 6 7) ( 38 50) ( 21 22)
( 11 12) ( 25 49) ( 4 5) ( 8 48) ( 28 29) ( 20 21)
( 12 13) ( 35 36) ( 34 35) ( 48 49) ( 53 54) ( 58 1)
( 30 31) ( 2 3) ( 3 51) ( 31 32) ( 35 58) ( 14 53)
( 6 28) ( 15 16) ( 42 43) ( 45 46) ( 13 14) ( 25 26)
( 5 6) ( 1 9) ( 10 11) ( 13 46) ( 38 39) ( 23 24)
( 11 19) ( 55 56) ( 4 45)
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Chromatic polynomial relative the tree basis:

$$\begin{aligned}
P(9 - CAGE - 15, x) = & \\
& +1x * (x - 1)^{57} \\
& -30x * (x - 1)^{56} \\
& +465x * (x - 1)^{55} \\
& -4960x * (x - 1)^{54} \\
& +40920x * (x - 1)^{53} \\
& -278256x * (x - 1)^{52} \\
& +1623160x * (x - 1)^{51} \\
& -8347680x * (x - 1)^{50} \\
& +38607928x * (x - 1)^{49} \\
& -163008778x * (x - 1)^{48} \\
& +635699476x * (x - 1)^{47} \\
& -2311295128x * (x - 1)^{46} \\
& +7894342286x * (x - 1)^{45} \\
& -25488485352x * (x - 1)^{44} \\
& +78197165382x * (x - 1)^{43} \\
& -228949151250x * (x - 1)^{42} \\
& +642048200309x * (x - 1)^{41} \\
& -1729833099890x * (x - 1)^{40} \\
& +4489138854155x * (x - 1)^{39} \\
& -11245424824164x * (x - 1)^{38} \\
& +27240560225622x * (x - 1)^{37} \\
& -63902492452342x * (x - 1)^{36} \\
& +145342204419607x * (x - 1)^{35} \\
& -320802054497891x * (x - 1)^{34} \\
& +687625210170725x * (x - 1)^{33} \\
& -1431989385001040x * (x - 1)^{32} \\
& +2898128370037524x * (x - 1)^{31} \\
& -5700574018802922x * (x - 1)^{30} \\
& +10896728904657243x * (x - 1)^{29} \\
& -20236053060653036x * (x - 1)^{28} \\
& +36492700869816596x * (x - 1)^{27} \\
& -63864239796654607x * (x - 1)^{26} \\
& +108373497210891182x * (x - 1)^{25} \\
& -178140362984653795x * (x - 1)^{24} \\
& +283302097510374499x * (x - 1)^{23} \\
& -435279200576107859x * (x - 1)^{22} \\
& +645059167892726840x * (x - 1)^{21} \\
& -920275602645303909x * (x - 1)^{20} \\
& +1261170473730410584x * (x - 1)^{19} \\
& -1656073003741391921x * (x - 1)^{18} \\
& +2077726186313686925x * (x - 1)^{17} \\
& -2482384186071794171x * (x - 1)^{16} \\
& +2813667939657840768x * (x - 1)^{15} \\
& -3012255947073894328x * (x - 1)^{14} \\
& +3030431300031960958x * (x - 1)^{13} \\
& -2847761853378906180x * (x - 1)^{12} \\
& +2481996910675361647x * (x - 1)^{11} \\
& -1989276334917383795x * (x - 1)^{10} \\
& +1451049291558079236x * (x - 1)^9 \\
& -951006007142760574x * (x - 1)^8 \\
& +550963034749725166x * (x - 1)^7 \\
& -276215106273780148x * (x - 1)^6 \\
& +116400254092257008x * (x - 1)^5 \\
& -39541762400292418x * (x - 1)^4 \\
& +10138173327479188x * (x - 1)^3 \\
& -1741046422181200x * (x - 1)^2 \\
& +149895790352224x * (x - 1)^1
\end{aligned}$$

Chromatic polynomial relative the standard basis:

$$\begin{aligned}
P(9 - Cage - 15, x) = & \\
& -29763162413230015248x \\
& +419813193274134413612x^2 \\
& -2980508193027530114116x^3 \\
& +14214379879109904226925x^4 \\
& -51262275589893762194970x^5 \\
& +149175247774850086623624x^6 \\
& -364946253793919942942846x^7 \\
& +772012495809851540317139x^8 \\
& -1441327821703675314268787x^9 \\
& +2411821085934201485592618x^{10} \\
& -3660748874632409539233297x^{11} \\
& +5088063036994395735661251x^{12} \\
& -6525258563418948448819415x^{13} \\
& +7769387539975520537618789x^{14} \\
& -8631941723044154251597684x^{15} \\
& +8985769461799381110180824x^{16} \\
& -8794167919768038248793377x^{17} \\
& +8113807783477578788616661x^{18} \\
& -7073199297457127169850633x^{19} \\
& +5836413419143844474451268x^{20} \\
& -4564858977234907622138073x^{21} \\
& +3387886229265605158038131x^{22} \\
& -2387780838875793871390219x^{23} \\
& +1599037022180272985443344x^{24} \\
& -1017788983990915338709418x^{25} \\
& +615802654838537563606714x^{26} \\
& -354144228191212905919387x^{27} \\
& +193540127014565162778242x^{28} \\
& -100471678175494033847921x^{29} \\
& +49518006873503309874279x^{30} \\
& -23154332597313014673822x^{31} \\
& +10263423390381969352276x^{32} \\
& -4308463704981059485497x^{33} \\
& +1710955120777805608272x^{34} \\
& -641933399770249099954x^{35} \\
& +227224259483161580455x^{36} \\
& -75758958985233193788x^{37} \\
& +23748944597807269226x^{38} \\
& -6985659611881615954x^{39} \\
& +1923702922602076094x^{40} \\
& -494684301414334022x^{41} \\
& +118448006205564332x^{42} \\
& -26322082620085850x^{43} \\
& +5408679817479600x^{44}
\end{aligned}$$

Roots of the chromatic polynomial of 9-CAGE-15:

$x - > 0.$	$x - > 1.63484 + 1.68942I$
$x - > 1.$	$x - > 1.78325 - 1.61714I$
$x - > 2.$	$x - > 1.78325 + 1.61714I$
$x - > 2.68465$	$x - > 1.92497 - 1.53304I$
$x - > -0.668264 - 1.15132I$	$x - > 1.92497 + 1.53304I$
$x - > -0.668264 + 1.15132I$	$x - > 2.05281 - 1.44835I$
$x - > -0.41277 - 1.3898I$	$x - > 2.05281 + 1.44835I$
$x - > -0.41277 + 1.3898I$	$x - > 2.16419 - 1.36078I$
$x - > -0.179574 - 1.53742I$	$x - > 2.16419 + 1.36078I$
$x - > -0.179574 + 1.53742I$	$x - > 2.25434 - 1.26988I$
$x - > 0.0381809 - 1.6455I$	$x - > 2.25434 + 1.26988I$
$x - > 0.0381809 + 1.6455I$	$x - > 2.32488 - 1.16081I$
$x - > 0.245858 - 1.7359I$	$x - > 2.32488 + 1.16081I$
$x - > 0.245858 + 1.7359I$	$x - > 2.39556 - 1.03341I$
$x - > 0.447932 - 1.81447I$	$x - > 2.39556 + 1.03341I$
$x - > 0.447932 + 1.81447I$	$x - > 2.46539 - 0.899768I$
$x - > 0.644098 - 1.87481I$	$x - > 2.46539 + 0.899768I$
$x - > 0.644098 + 1.87481I$	$x - > 2.52921 - 0.762654I$
$x - > 0.825162 - 1.8937I$	$x - > 2.52921 + 0.762654I$
$x - > 0.825162 + 1.8937I$	$x - > 2.5848 - 0.628049I$
$x - > 0.995619 - 1.88071I$	$x - > 2.5848 + 0.628049I$
$x - > 0.995619 + 1.88071I$	$x - > 2.6288 - 0.497498I$
$x - > 1.16114 - 1.84838I$	$x - > 2.6288 + 0.497498I$
$x - > 1.16114 + 1.84838I$	$x - > 2.65742 - 0.369095I$
$x - > 1.32217 - 1.80391I$	$x - > 2.65742 + 0.369095I$
$x - > 1.32217 + 1.80391I$	$x - > 2.67435 - 0.242902I$
$x - > 1.48079 - 1.75144I$	$x - > 2.67435 + 0.242902I$
$x - > 1.48079 + 1.75144I$	$x - > 2.68251 - 0.120138I$
$x - > 1.63484 - 1.68942I$	$x - > 2.68251 + 0.120138I$