

*****9-CAGE-5*****

Edges of 9-CAGE-5:

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( 31 32) ( 25 40) ( 54 55) ( 30 31) ( 56 57) ( 24 25)
( 41 42) ( 26 27) ( 5 6) ( 55 56) ( 10 11) ( 12 13)
( 4 46) ( 28 29) ( 37 38) ( 2 27) ( 35 48) ( 33 34)
( 29 43) ( 9 10) ( 8 42) ( 26 53) ( 23 31) ( 47 48)
( 39 57) ( 5 38) ( 19 34) ( 13 14) ( 53 54) ( 52 53)
( 19 20) ( 14 32) ( 11 37) ( 2 3) ( 16 17) ( 45 46)
( 23 24) ( 1 9) ( 28 36) ( 50 51) ( 39 40) ( 18 19)
( 43 44) ( 13 45) ( 35 36) ( 3 17) ( 44 45) ( 49 58)
( 51 52) ( 32 33) ( 22 23) ( 16 41) ( 6 52) ( 18 55)
( 1 2) ( 12 54) ( 4 5) ( 21 51) ( 57 58) ( 29 30)
( 27 28) ( 36 37) ( 48 49) ( 58 1) ( 25 26) ( 8 9)
( 49 50) ( 6 7) ( 7 33) ( 20 21) ( 17 18) ( 21 22)
( 3 4) ( 7 8) ( 34 35) ( 20 44) ( 42 43) ( 46 47)
( 15 50) ( 11 12) ( 38 39) ( 40 41) ( 15 16) ( 24 47)
( 10 22) ( 30 56) ( 14 15)
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Chromatic polynomial relative the tree basis:

$$\begin{aligned}
P(9 - CAGE - 5, x) = & \\
& +1x * (x - 1)^{57} \\
& -30x * (x - 1)^{56} \\
& +465x * (x - 1)^{55} \\
& -4960x * (x - 1)^{54} \\
& +40920x * (x - 1)^{53} \\
& -278256x * (x - 1)^{52} \\
& +1623160x * (x - 1)^{51} \\
& -8347680x * (x - 1)^{50} \\
& +38607936x * (x - 1)^{49} \\
& -163008999x * (x - 1)^{48} \\
& +635702638x * (x - 1)^{47} \\
& -2311326325x * (x - 1)^{46} \\
& +7894580690x * (x - 1)^{45} \\
& -25489988164x * (x - 1)^{44} \\
& +78205292728x * (x - 1)^{43} \\
& -228987881060x * (x - 1)^{42} \\
& +642213985832x * (x - 1)^{41} \\
& -1730479822102x * (x - 1)^{40} \\
& +4491463746109x * (x - 1)^{39} \\
& -11253195015073x * (x - 1)^{38} \\
& +27264875756451x * (x - 1)^{37} \\
& -63974150364260x * (x - 1)^{36} \\
& +145542018978192x * (x - 1)^{35} \\
& -321331308866645x * (x - 1)^{34} \\
& +688961099883070x * (x - 1)^{33} \\
& -1435211136398494x * (x - 1)^{32} \\
& +2905568232472643x * (x - 1)^{31} \\
& -5717053537541651x * (x - 1)^{30} \\
& +10931790202999565x * (x - 1)^{29} \\
& -20307778237287030x * (x - 1)^{28} \\
& +36633890788621135x * (x - 1)^{27} \\
& -64131807080251015x * (x - 1)^{26} \\
& +108861760102768260x * (x - 1)^{25} \\
& -178998281986467526x * (x - 1)^{24} \\
& +284753122843286391x * (x - 1)^{23} \\
& -437640124312060369x * (x - 1)^{22} \\
& +648751305335536127x * (x - 1)^{21} \\
& -925818407012631513x * (x - 1)^{20} \\
& +1269145730657304424x * (x - 1)^{19} \\
& -1667049238684023791x * (x - 1)^{18} \\
& +2092140263420062109x * (x - 1)^{17} \\
& -2500391624998367872x * (x - 1)^{16} \\
& +283493533190722089x * (x - 1)^{15} \\
& -3036095313976166658x * (x - 1)^{14} \\
& +3055460832688892282x * (x - 1)^{13} \\
& -2872297104202287858x * (x - 1)^{12} \\
& +2504293062339214995x * (x - 1)^{11} \\
& -2007900374210675197x * (x - 1)^{10} \\
& +1465201486332687600x * (x - 1)^9 \\
& -960664440108058838x * (x - 1)^8 \\
& +556787456529636308x * (x - 1)^7 \\
& -279253269607077490x * (x - 1)^6 \\
& +117731827607007136x * (x - 1)^5 \\
& -40011973611863711x * (x - 1)^4 \\
& +10263409774398510x * (x - 1)^3 \\
& -1763367407929505x * (x - 1)^2 \\
& +151887710184306x * (x - 1)^1
\end{aligned}$$

Chromatic polynomial relative the standard basis:

$$\begin{aligned}
P(9 - Cage - 5, x) = & \\
& -29999747832407984144x \\
& +422994188514924479236x^2 \\
& -3001996947964029303988x^3 \\
& +14311705461823583833599x^4 \\
& -51594893646318193809778x^5 \\
& +150090268457555951472130x^6 \\
& -367056418202499624843279x^7 \\
& +776206502068003921600587x^8 \\
& -1448656394380828616235654x^9 \\
& +2423248261690131158743096x^{10} \\
& -3676830315540287121408812x^{11} \\
& +5108670603617867243997118x^{12} \\
& -6549473593031462437525817x^{13} \\
& +7795625130351576502831509x^{14} \\
& -8658273874061541301203798x^{15} \\
& +9010335308685159352194652x^{16} \\
& -8815533216328352170730292x^{17} \\
& +8131170198698582658497540x^{18} \\
& -7086406542777187390319938x^{19} \\
& +5845830323537104374169936x^{20} \\
& -4571158838230126791634844x^{21} \\
& +3391843287033935670397569x^{22} \\
& -2390115354904274059344389x^{23} \\
& +1600330776949528951738073x^{24} \\
& -1018462388317195563584082x^{25} \\
& +616131735472170831131066x^{26} \\
& -354295119000986063691040x^{27} \\
& +193604988509959978789936x^{28} \\
& -100497787794439102271411x^{29} \\
& +49527836133974861450474x^{30} \\
& -23157787611475946489610x^{31} \\
& +10264555175877690342103x^{32} \\
& -4308808452881392735202x^{33} \\
& +1711052517407421807182x^{34} \\
& -641958844237591027379x^{35} \\
& +227230385008285486996x^{36} \\
& -75760312426854597045x^{37} \\
& +23749217765345317129x^{38} \\
& -6985709695148381694x^{39} \\
& +1923711208741901662x^{40} \\
& -494685528694015448x^{41} \\
& +118448167356709225x^{42} \\
& -26322101153310837x^{43} \\
& +5408681655600936x^{44}
\end{aligned}$$

Roots of the chromatic polynomial of 9-CAGE-5:

$$\begin{aligned}
x- > 0. & \quad x- > 1.63547 + 1.68894I \\
x- > 1. & \quad x- > 1.78652 - 1.6172I \\
x- > 2. & \quad x- > 1.78652 + 1.6172I \\
x- > 2.68223 & \quad x- > 1.92875 - 1.53397I \\
x- > -0.67063 - 1.15242I & \quad x- > 1.92875 + 1.53397I \\
x- > -0.67063 + 1.15242I & \quad x- > 2.05742 - 1.45692I \\
x- > -0.412536 - 1.38839I & \quad x- > 2.05742 + 1.45692I \\
x- > -0.412536 + 1.38839I & \quad x- > 2.15658 - 1.37331I \\
x- > -0.179126 - 1.53545I & \quad x- > 2.15658 + 1.37331I \\
x- > -0.179126 + 1.53545I & \quad x- > 2.24104 - 1.26826I \\
x- > 0.0381671 - 1.64606I & \quad x- > 2.24104 + 1.26826I \\
x- > 0.0381671 + 1.64606I & \quad x- > 2.32304 - 1.15056I \\
x- > 0.245687 - 1.73782I & \quad x- > 2.32304 + 1.15056I \\
x- > 0.245687 + 1.73782I & \quad x- > 2.4009 - 1.02514I \\
x- > 0.447413 - 1.81593I & \quad x- > 2.4009 + 1.02514I \\
x- > 0.447413 + 1.81593I & \quad x- > 2.47278 - 0.895149I \\
x- > 0.643902 - 1.87694I & \quad x- > 2.47278 + 0.895149I \\
x- > 0.643902 + 1.87694I & \quad x- > 2.53572 - 0.763051I \\
x- > 0.824066 - 1.89412I & \quad x- > 2.53572 + 0.763051I \\
x- > 0.824066 + 1.89412I & \quad x- > 2.58807 - 0.631199I \\
x- > 0.994636 - 1.8791I & \quad x- > 2.58807 + 0.631199I \\
x- > 0.994636 + 1.8791I & \quad x- > 2.62902 - 0.501541I \\
x- > 1.15975 - 1.84666I & \quad x- > 2.62902 + 0.501541I \\
x- > 1.15975 + 1.84666I & \quad x- > 2.65708 - 0.37448I \\
x- > 1.32188 - 1.80304I & \quad x- > 2.65708 + 0.37448I \\
x- > 1.32188 + 1.80304I & \quad x- > 2.67245 - 0.248533I \\
x- > 1.48088 - 1.7507I & \quad x- > 2.67245 + 0.248533I \\
x- > 1.48088 + 1.7507I & \quad x- > 2.67995 - 0.123538I \\
x- > 1.63547 - 1.68894I & \quad x- > 2.67995 + 0.123538I
\end{aligned}$$