Thermodynamics & Statistical Mechanics

Worksheet For Class 09/05 (Interacting Einstein Solids)

1. Binomial Coefficient

In the following we will use EXCEL (in linux use libreoffice) to determine multiplicities and therefore we will need the EXCEL command for $\begin{pmatrix} a \\ b \end{pmatrix}$, so "a choose b", or the binomial coefficient. Use the command COMBIN(a,b) in EXCEL for $\Omega(N = 3, q = 6) = \begin{pmatrix} 8 \\ 6 \end{pmatrix}$ and check if you get the expected result (see solutions to today's homework #6).

2. Einstein Solids $N_A = N_B = 3$ $q_{tot} = q_A + q_B = 6$

(Problem 2.9) Use EXCEL to reproduce Fig. 2.4 (table & graph) on page 57, so for two Einstein solids with $N_A = N_B = 3$ $q_{tot} = q_A + q_B = 6$. At the beginning of your table set the parameters N_A , N_B , and q_{tot} and refer to these parameters with absolute references in your table.

3. Einstein Solids $N_A = 6$ $N_B = 4$ $q_{tot} = q_A + q_B = 6$

(Problem 2.9 continued) Modify your table and graph to show the case $N_A = 6$ $N_B = 4$ $q_{\text{tot}} = q_A + q_B = 6$. Assuming that all microstates are equally likely, what is the most probable macrostate, and what is its probability? What is the least probable macrostate, and what is its probability?

4. Einstein Solids $N_A = 60$ $N_B = 40$ $q_{tot} = q_A + q_B = 60$

Now let's just scale up our system size. Modify your table and graph to show the case $N_A = 60$ $N_B = 40$ $q_{\text{tot}} = q_A + q_B = 60$. Compare the resulting graph with your result in 3.

5. (if time)

Try to increase the size even more, so $N_A = 300$ $N_B = 200$ $q_{tot} = q_A + q_B = 300$.

6. (if time)

What happens if you increase the size to $N_A = 600$ $N_B = 400$ $q_{tot} = q_A + q_B = 600$?

Read: §2.4 **Homework #7:** 2.10 & 2.11