

# Useful Integrals

$$\int \frac{x dx}{(a^2 + x^2)^{3/2}} = \frac{-1}{\sqrt{a^2 + x^2}}; \quad \int \frac{dx}{(a^2 + x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2 + x^2}};$$

$$\int \sin^2(ax) dx = \frac{x}{2} - \frac{1}{4a} \sin(2ax)$$

$$\int x \sin^2(ax) dx = \frac{x^2}{4} - \frac{x}{4a} \sin(2ax) - \frac{1}{8a^2} \cos(2ax)$$

$$\int e^{-bx} dx = -e^{-bx} \left(\frac{1}{b}\right); \quad \int x e^{-bx} dx = -e^{-bx} \left(\frac{x}{b} + \frac{1}{b^2}\right)$$

$$\int x^2 e^{-bx} dx = -e^{-bx} \left(\frac{x^2}{b} + \frac{2x}{b^2} + \frac{2}{b^3}\right)$$