## In-Class Work: Traffic Flow

## 6. Update Positions

If you had at the end of last class finished step 5, that is the update of all velocities, then you may continue with your program from last class. If you had not finished step 5, please copy the program
~kvollmay/share.dir/inclass2019.dir/traffic5.py into your working directory, and use this program as starting program for today's inclass work.

Add to the program the update of the positions. To do so use a new loop over all cars and update both the carpos array and the road array. For the update of road make sure to first copy the new velocity into a variable (e.g. vnew), then empty the old site and then put the car in road on its new site xnew = xold + vnew with the new velocity (the order of these commands matters). After the update of all positions print the complete road and check if it is what you expected. Using the same parameters as in traffic5.py ${ }^{3}$ compare your result with
~kvollmay/share.dir/inclass2019.dir/traffic6_PCAR03.data

## 7. Finish Program

Now you are set to finish the program for our traffic flow model. Add to your program from 6. the time loop. Compare your result for the case of 100 timesteps (MAXTIMESTEPS $=100$ ), and the same parameters as in step 5 (see footnote). Compare your output with ~kvollmay/share.dir/inclass2019.dir/traffic7_PCAR03.data

## 8. Space-Time Diagrams

8a. Now we are ready to have a look at the flow of the cars. Next we will make a so called space-time diagram. This is an image of the road for successive time timesteps, i.e. on the $x$-axis is the road position and the $y$-axis is downwards and equal to the number of time steps. You find an example in Fig. 3 of the Chowdhury et al. traffic flow paper. This means that we want a picture similar to the DLA-fractal growth picture we made in class when we worked on the DLA model. You will need to first make a two-dimensional array which stores the space-time diagram data, for example named spacetimearray

Add to your program such an array and set the values of the spacetimearray during your time-loop. To print the array at the end into a file, you may use the following lines:

[^0]```
#print spacetimearray into file
fileoutdat=open("spacetime8.data",mode='w')
for i in range(MAXTIMESTEPS):
    for j in range(ROADLENGTH):
            print(spacetimearray[i,j], end=" ",file=fileoutdat)
    print("\n", end=" ",file=fileoutdat)
fileoutdat.close()
```

To test your program compare the resulting spacetime8. data with your results in step 7 .
8 b . To be able to see the main patterns (and to get nice pictures) use a larger road ROADLENGTH= 200. Now you are ready to make a nice picture of this space-time diagram. You can do this with the following line at the beginning of your program import matplotlib.pyplot as plt (which was inlcuded in traffic5.py) and at the end of the program with:
plt.imshow(spacetimearray,interpolation='nearest')
plt.colorbar(ticks=[0, 1, 2, 3, 4, 5], orientation='horizontal')
Look at the resulting space-time diagram and interpret it.
8b. To distinguish stopped cars easily from driving cars, let's indicate every empty site instead of with -1 now with -VMAX. Look at the space-time diagram.
8c. Vary PCAR. Interpret the resulting space-time diagrams. Once you have several spacetime diagrams for different PCAR, get me so that we can discuss as a class your results.

## 9. Nagel-Schreckenberg Model

9a. Get me when you get to this part. We are now ready to finish the programming of the Nagel-Schreckenberg model. Add to your program of 8. the randomization of the velocity, so complete the Nagel-Schreckenberg Model. Use VMAX $=5$, $\operatorname{PCAR}=0.2$, $\operatorname{PDEC}=0.25$, ROADLENGTH $=200$, MAXTSTEPS=100 and have a look at the resulting space-time diagram.
9b. Keep all parameters as in 9a but vary
(i) PCAR between 0.05 and 0.35
(ii) PDEC between 0.0 and 0.5
(iii) VMAX between 1 and 10 .

What do you observe in each case? Please get me to discuss your observations and to share your results with the class.

## 10. Mean Velocity $v_{\text {av }}(t)$

Use your program from 9. with parameters VMAX=5, PCAR=0.2, PDEC=0.25, ROADLENGTH=1000, and MAXTIMESTEPS=200 but after the time loop do not print out the space-time data and figure but instead print within the time loop one line with two numbers: time step t and $v_{\mathrm{av}}$ where $v_{\mathrm{av}}$ is the mean velocity:

$$
\begin{equation*}
v_{\mathrm{av}}(t)=\frac{1}{N} \sum_{i=0}^{N-1} v_{i}(t) \tag{1}
\end{equation*}
$$

$N$ is the number of cars and $v_{i}$ is the velocity of car $i$. Compare your result with ~kvollmay/share.dir/inclass2019.dir/traffic10out.data
Look at $v_{\mathrm{av}}(t)$ with:
traffic10.py | xmgrace -pipe
Get me so that we can discuss your result. Our interpretation will be necessary for next class.


[^0]:    ${ }^{3}$ road length $L=20, p_{\text {car }}=0.3, v_{\max }=5$ and sp.random.seed (15) +

