

# TOYS & TEA



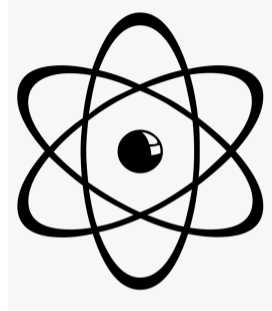
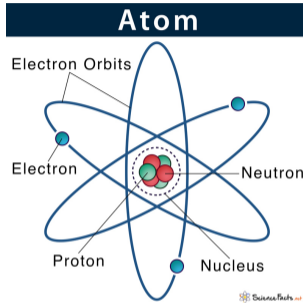
EVERY  
OTHER  
THURSDAY

4:00 - 5:00 PM

PHYSICS  
STUDENT LOUNGE  
OLIN 251A

COME AND EXPERIENCE FUN EXPERIMENTS WITH  
YOUR FAVORITE PHYSICS & ASTRONOMY FACULTY

Common picture of an atom:



This kind of atom could not exist! The accelerating electron would radiate away all of its energy as an EM wave, and then crash into the nucleus.

**Classical mechanics + E&M  $\Rightarrow$  atoms can't exist!!**

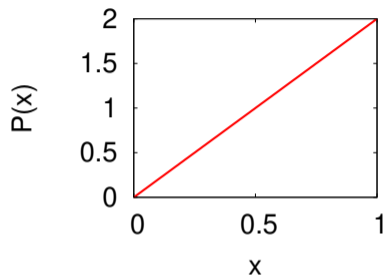
...but fortunately atoms **do** exist. We have to give up on classical mechanics to explain them.

## Lecture 15 — Concept Test 1

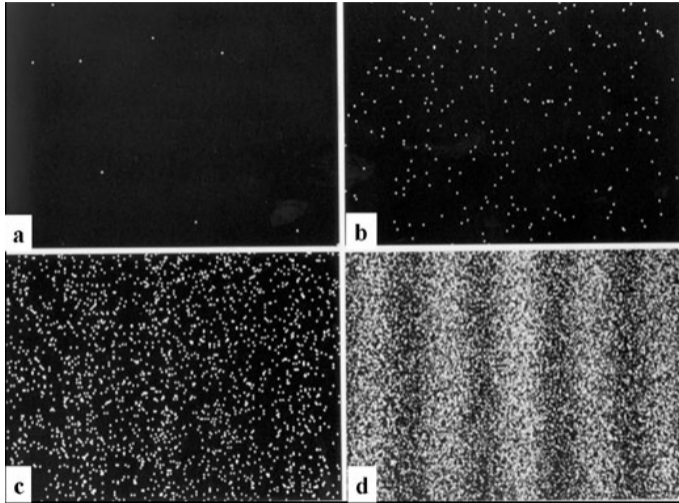
A particle is associated with a probability density  $P(x) = 2x$  from  $x = 0$  to  $x = 1$ , and  $P(x) = 0$  for all other values of  $x$ .

What is the probability that the particle would be found between  $x = 0$  and  $x = 1/2$ ?

- |          |          |
|----------|----------|
| 1. 0     | 4. $1/2$ |
| 2. $1/8$ | 5. 1     |
| 3. $1/4$ | 6. 2     |



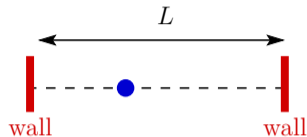
# Electron Double Slit Experiment



<https://www.hitachi.com/rd/research/materials/quantum/doubleslit/index.html>

## Lecture 15 — Concept Test 2

You trap a particle in a very small 1D box such that the spread in position  $\sigma_x$  must be quite small. What does Heisenberg's Uncertainty Principle imply about this particle?



Answer each statement with **1 = True** or **2 = False**.

- A. A small spread in position  $\sigma_x$  implies a small spread in momentum  $\sigma_{p_x}$  (and therefore velocity).
- B. There is a minimum kinetic energy greater than zero that the particle must have.
- C. If we make the box smaller, the kinetic energy of the particle becomes smaller

## Lecture 15 — Concept Test 3

Given the equation  $\frac{df(x)}{dx} + 6x - 2 = 0$ , test the trial solution

$$f(x) = Ax + B$$

to see if it works. If so, determine the values of the constants  $A$  and  $B$  needed to make it work.

1. This doesn't work for all values of  $x$ .
2. Works if  $A = 6$  and  $B = -2$
3. Works if  $A = -6$  and  $B = 2$ .
4. Works if  $A = 2$  and  $B = -6$
5. Works if  $A = -2$  and  $B = 6$
6. Works if  $A = \pi$  and  $B = \sqrt{17}$ .

## Lecture 15 — Concept Test 4

Given the equation  $\frac{df(x)}{dx} + 6x - 2 = 0$ , test the trial solution

$$f(x) = Ax^2 + Bx + C$$

to see if it works. If so, determine the values of the constants  $A$ ,  $B$ , and  $C$  needed to make it work.

1. This doesn't work for all values of  $x$ .
2. Works if  $A = 6$ ,  $B = -2$ , and  $C = 0$
3. Works if  $A = -6$ ,  $B = 2$ , and  $C$  can be anything
4. Works if  $A = 3$ ,  $B = -2$ , and  $C = 0$
5. Works if  $A = -3$ ,  $B = 2$ , and  $C$  can be anything
6. Works if  $A = \pi$ ,  $B = \sqrt{17}$ , and  $C = \sqrt{-1}$ .

## Simple Harmonic Motion

## Schrödinger Equation for $U = 0$

**Equation:** 
$$\frac{d^2 y(t)}{dt^2} = -\frac{k_{\text{sp}}}{m} y(t)$$

$$\frac{d^2 \psi(x)}{dx^2} = -\frac{2mE}{\hbar^2} \psi(x)$$

**Solution:** 
$$y(t) = A \sin(\omega t + \phi_0)$$

$$\psi(x) = A \sin(kx + \phi_0)$$

$$\text{where } \omega = \sqrt{\frac{k_{\text{sp}}}{m}}$$

$$\text{where } k = \sqrt{\frac{2mE}{\hbar^2}}$$

Check if Schrödinger's Equation matches de Broglie relation for  $U = 0$ :

$$E = K + \cancel{U}^0 = \frac{1}{2}mv^2 = \frac{p^2}{2m} \quad \Rightarrow \quad p = \sqrt{2mE}.$$

$$\text{de Broglie: } \lambda = \frac{h}{p} \quad \Rightarrow \quad k = \frac{2\pi}{\lambda} = \frac{2\pi p}{h} = \frac{p}{\hbar} = \sqrt{\frac{2mE}{\hbar^2}} \quad \checkmark$$