

TOMIC LABORATORIES, INC., 3086 Claremont Ave., Berkeley 5, California

Subsidiary Cenco Instruments Corporation

### M-4 INTERFEROMETER

#### OPERATION AND EXPERIMENT MANUAL

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#### PART 1

#### MICHELSON OPTICS

The Atomic Laboratories M-4 Interferometer is fabricated with Michelson Optics, with Fabry-Ferot Optics, or with a combination of both. The Michelson front surface mirrors and beam splitter and the Fabry-Ferot mirrors must be treated with the utmost respect. They are never to be touched without wearing gloves, and then only sparingly. Dust may be cleaned from the mirrors by means of the camel's hair brush which is shipped with each instrument. Other matter may be removed, if absolutely necessary, with a soft cloth or piece of lens paper brushed ever so lightly against the surface. When the interferometer is stored, it should be covered at all times with the plastic bag. It is also a good idea to keep the lens covers over the optics when they are not in use.

When the M-4 Interferometer is ordered with only one set of optics, the other set may be ordered at any future date and easily installed by removing the masking tape on the interferometer chassis and carriage and inserting the screws in the indicated noise. The following unpacking instructions apply to the interferometer irregardless of the type of optics.

<u>Unpacking</u>: Gently remove the cardboard insert which holds the interferometer in place, being extremely careful not to rub or push it against the optics while lifting it out. Place the interferometer on a level surface and remove the plastic cover, as well as the lens covers. Remove the tape which holds the carriage in place.

Light Source: The M-4 Interferometer will operate with any standard mercury or sodium light source, including Atomic Laboratories' own monochromatic mercury light source. To operate the source, insert lamp, either one or both of the two diffuser plates, and, if desired, the green Wratten filter. If used with the Michelson Optics, the light source should be positioned as shown in the photograph. The light should enter the beam splitter at a 45° angle. DANGER: ULTRAVIOLET RAYS CAN

SEVERELY DAMAGE THE EYE. THE DIFFUSER PLATES ABSORB THESE RAYS: IF THEY SHOULD BE REMOVED OR BROKEN, THE EXPOSED LAMP BECOMES EXTREMELY DANGEROUS:





Adjustment: Move the carriage until mirror number 2 is approximately the same distance from the beam splitter as the fixed mirror number 1. This distance is generally about 12.5 cm., but it should be checked with a ruler. It should be measured from the coated side (left side) of the beam splitter in each case. Now tighten the carriage lock screw to hold the carriage firmly in place. Turn on the light source, which is in the position previously described. The next step is to bring the mirrors into exact perpendicularity. The adjustment can be accomplished as follows:

Turn on the light source and observe the focusing pin\* which is situated between the light source and the beam splitter. Two images of the pin will be seen, one coming from the reflection at the front surface of the beam splitter, the other from the reflection at its back surface.

Line up the vertical positions of the focusing pin. This can be done by means of the adjusting screw of mirror number 1. The adjusting screw of mirror number 2 will line up the focusing pin horizontally. When only one image of the pin is achieved, fringes should appear. To best observe these fringes, look straight into the back mirror from the front of the interferometer.

It takes a little practice to obtain the fringes. As stated previously, before touching the adjusting screws, make certain that the two mirrors are equally distant from the beam solitter. When the fringes first appear they can be sharpened by very careful and minute adjustment of the screws. If the adjustment is accomplished in a room with a great deal of vibration or on an unsteady table, the fringes will soon disappear.

Often only very thin and blurred fringes will be seen in the beginning. A good technique is to line them up vertically or horizontally (see below) by adjusting one mirror. Then by centering in with the other mirror, the fringe curvature will be increased until finally the center appears. Be sure while making these adjustments that the mirror is moved in the direction of the fringe's decreased radius of curvature.



Decrease radius



Finally-the bull's-eye

<u>MAINTENANCE</u>: Every six months remove carriage and wipe steel ways with clean rag containing a few drops of three-in-one oil. Ways must be spotlessly clean and free of dust, dirt, or rust for efficient operation.

of curvature

### EXPERIMENT 1: Determination of the Wave Length of Monochromatic Light.

<u>Procedure</u>: Use Atomic Laboratories' Mercury Light Source, with a Wratten Number 74 filter or equivalent. Once a good pattern of fringes has been obtained, take a reading of the micrometer head. By turning the head, the carriage can be moved slowly in either direction. Count the fringes as they pass by the focusing pin or as they appear or disappear in the bull'seye. For satisfactory precision, count at least one hundred fringes. After counting them off, take a new reading of the micrometer head. From the number of fringes passed over,  $\Delta n$ , and the distance traversed by the mirror, we may determine the wave length of the monochromatic light by means of

<sup>\*</sup> The focusing pin is removable from the carriage.

the formula:

$$2(d_1 - d_2) = \lambda \Delta n$$

The distance travelled by the mirror in centimeters is given by

$$(d_1 - d_2) = 0.10 (D_1 - D_2) \times K$$

:

where  $(D_1 - D_2)$  is the change of the micrometer reading in millimeters and K is the ratio of carriage movement to micrometer screw reading. For the M-4 Interferometer K = 0.020

Whence:

$$\lambda = \frac{2(0,10)(D_1 - D_2)K}{\Delta n} \quad \text{cm.}$$

The correct value for the wavelength of green mercury light is 5460.740 Å ( $1 \text{ Å} = 1 \times 10^{-3} \text{ cm}$ ). You may wish to use this correct value of the wavelength to obtain a more exact value for K, since there are some variations in manufacturing conditions of the instrument.

<u>Discussion</u>: An Interferometer is generally defined as an optical instrument which produces interference patterns by the division of one beam of light into one or more parts. These parts travel different paths and are then ultimately brought together to yield the interference effects. The resultant patterns depend on the optical paths traversed by the several beams. Consequently, the Interferometer determines <u>differences in optical paths</u>. Since the optical path is the product of refractive index  $\mu$  by path length d, it is clear that if the several beams traverse media of the same  $\mu$ , a measure of the path length d is given. Conversely, if the path lengths d are equal (or at least constant) then the refractive index is determined. Thus, the Interferometer may be used to measure any of these three quantities: (1) Geometrical path length, (2) Optical path length, (3) Refractive index.

Determination of optical path length is of importance in technical applications. Measurement of indices of refraction will be the subject of experiments numbers 4 and 5. In this experiment, however, we have been concerned with geometrical path length.

If the difference between the separations of the two full-silvered mirrors from the half-silvered one (beam splitter) is d, then the difference of geometrical path length for the two central (normal) rays is 2d, because the distance d is traversed once in each direction. Consequently, the condition for constructive interference for the central rays is:

## 2d = nλ

Where  $\lambda$  is the wave length of the light and n is an integer. Actually because of the difference between internal and external reflections at silvered surfaces a phase reversal of one of the rays may result, in which case the above condition would be appropriate to destructive interference, and that for constructive interference would be:

$$2d = (n + 1/2)\lambda$$

Since we measure fringe shifts here, which condition applies is of no consequence and the formula which is applicable is:

2 
$$(d_1 - d_2) = \lambda \Delta n$$

Where  $(d_1 - d_2)$  is the distance the carriage is moved to cause the appearance or disappearance of  $\Delta n$  fringes at the center.

Using the calibration given above and the readings of the micrometer head (before and after carriage motion) the wave length is determined by use of the above formula, by substituting the appropriate values of  $(d_1 - d_2)$  and  $\Delta n$  into it.

#### EXPERIMENT 2: Measurement of Sodium Coublet Separation.

<u>Procedure</u>: The sodium doublet consists of two yellow spectral lines, having wavelengths of 5890 and 5896 A. The 5890 A line is twice as intense as the 5896 A line.

Use a sodium light source (e.g. Cenco Number 87300) to establish a straight line fringe pattern. There are now two sets of fringe patterns formed, one for each line of the doublet. Loosen the carriage lock screw and move the carriage by hand and observe that the yellow fringes pass alternately from a condition of high contrast to one of almost complete disappearance. This latter condition occurs when one set of fringes is half way between the other set. Fix the carriage at one of the conditions of most complete disappearance by tightening the carriage lock screw and read the micrometer head. By turning the micrometer head, move to the next condition of most complete disappearance and read the head again. Repeat. Calculate the average distance <u>d</u> between conditions of disappearance. We can now calculate the difference in wavelengths of these two lines as follows:

At the first micrometer reading:

$$2d_1 = m_1\lambda_1 = (m_1 + n + 1/2) \lambda_2$$

Where  $\lambda_1$  is greater than  $\lambda_2$ . The term on the right hand side indicates that the order of the shorter wavelength fringe differs from that of the longer wavelength fringe system by an odd half integer. This is true since the condition of disappearance of the fringe system occurs when one system is just halfway between the other. For the second reading, we have:

$$2 d_2 = m_2 \lambda_1 = (m_2 + n + 3/2) \lambda_2$$

By subtraction we obtain:

$$2(d_2 - d_1) = \frac{\lambda_1 \lambda_2}{\lambda_1 - \lambda_2}$$

Since  $\lambda_1$  and  $\lambda_2$  are approximately equal, we then obtain:

$$\lambda_1 - \lambda_2 = \Delta \lambda = \lambda^2/2d$$

Where X is the average wavelength, and  $d = d_2 - d_1 = 0.10 (D_2 - D_1)K$ .

The average wavelength can be measured by repeating Experiment 1 using the Sodium lamp as the light source.

#### EXPERIMENT 3: Observation of White Light Frinces.

<u>Frocedure</u>: In order to observe fringes with a source of white light, it is best to adjust the Interferometer to obtain the so-called localized fringes. This is done by adjusting one of the mirrors slightly so as to destroy the condition of exact perpendicularity. The fringe pattern now will consist of curved, horizontal or vertical stripes. Next, a position of nearly zero path length is searched for. This position is characterized by the fact that the striped pattern will become most nearly straight when the condition is achieved.

At this point an extended white light source may be substituted for the monochromatic source, and a very slow motion of the carriage will bring the white light fringes into view. White fringes are especially important in the Michelson Interferometer in that they give a precise indication of the position of zero optical path length difference.

An ordinary, frosted, incandescent lamp or even bright sunlight will serve very well as the light source for this experiment. The lamp can be placed behind the monochromatic light and turned on in the beginning of the experiment. When zero path length is obtained, simply turn off the monochromatic light.

Another means of obtaining zero path length is to construct a "T" by separating a diffuser plate with cardboard or black paper (see drawing). Place a monochromatic light source on one side, a white light source on the other, and turn both of them on. With this method it is not necessary to obtain localized fringes. Once any fringes have been obtained--they will appear in the left side of the mirror--loosen carriage lock screw and move carriage slowly by hand until the right side of the



mirror flashes briefly with color. Tighten carriage lock screw. Search either way from this direction, and the white light fringes, which have the appearance of small spectra, will be finally located.

<u>Discussion</u>: Only a few white light fringes are observed. This is accounted for when we recall that white light consists of all wave lengths of visible light. Apart from the central fringe, the various interference patterns (for different wave lengths) will overlap. A colored fringe is violet on the side nearer to the central fringe and red on the other.

# EXPERIMENT 4: Index of Refraction of a Transparent Solid.

<u>Procedure</u>: For the purpose of performing this experiment it will be necessary to construct a sample holder which is capable of positioning the sample accurately between the beam splitter and the fixed mirror (mirror number 1). The holder must be capable of giving a slow rotation of the sample, through a measureable angle.

When the holder has been attached to the Interferometer and with the sample positioned normal to the beam, the instrument is aligned to produce circular monochromatic fringes. When this has been achieved, rotate the sample through an angle sufficient to produce a shift of a few hundred fringes. Count the number of fringes. The index of refraction of the sample is then given by the formula:

:

where  $\Delta(\mu x)$  is the increase in optical path produced by the rotation.

For a given angle of rotation 0, fringe shift  $\Delta n$ , and wave length  $\lambda$ ,  $\mu$  is evaluated as follows:



 $\lambda \underline{\wedge n} = t \sqrt{\mu^2 - \sin^2 \theta} + t (1 - \cos \theta - \mu)$ 

$$t^{2} (\mu^{2} - \sin^{2}\theta) = \left(\frac{\lambda \Delta n}{2}\right)^{2} \div t^{2} (\mu^{2} \div \cos^{2}\theta + 1 \div 2\mu\cos\theta - 2\mu - 2\cos\theta) \\ + \lambda t \Delta n (\mu + \cos\theta - 1)$$

Neglecting the term  $\left(\lambda \frac{\Delta n}{2}\right)^2$  (because it is very small) and simplifying gives  $\mu = \frac{\lambda \Delta n}{(1 - 2)(1 - \cos \theta)}$ 

$$= \frac{(1 - 2)(1 - \cos \theta)}{t(1 - \cos \theta) - \lambda \Delta n}$$

Any transparent material available in suitable shape and size will be satisfactory. One must bear in mind that index of refraction depends on wave length and that, therefore, different results will be obtained for different colors of light.

#### EXPERIMENT 5: Index of Refraction of a Gas.

Procedure: For this experiment it is necessary to construct a gas cell with plane, flat transparent surfaces normal to the beam direction. The cell must be capable of being evacuated. It must also be possible to introduce the gas sample at a known temperature and pressure. It is, of course, necessary to introduce the sample sufficiently slowly that the fringe shift can be determined. The index of refraction of the gas is then given by

$$2(\mu - 1) + = \lambda \Delta n$$

where t is the geometrical path length through the cell. Here the quantity  $\mu$  depends on the pressure and temperature of the gas according to the Lorentz-Lorenz Law.

A simple gas cell has been described by T. G. Bullen in Am. J. Phys. <u>27</u>, 520 (1959). The following description is from his article:

A cell can be readily constructed from a piece of brass tubing about 4 cm in diameter and 6 to 7 cm long. The ends of the tubing should be turned true in a lathe and a side tube attached for pumping. Thin plate glass squares, carefully cleaned with alcohol, are then fitted to the ends with Tackiwax (Central Scientific Co., Catalog No. 11444). The cell is placed in the uncompensated arm of the interferometer and attached to a ballast bottle of about five-liters capacity, fitted with a stop cock for admitting air and for connection to a vacuum pump. On pumping down the system the fringe pattern alters in a staccato fashion, very rapidly at first and then more slowly as vacuum is attained. Leaks can be detected if the pattern is observed to alter when pumping is complete. By admitting air slowly through the stop-cock it is possible to count the fringe displacement from vacuum to atmospheric pressure. For gases other than air the determination can be made by admitting the gas via the stop-cock. The ballast bottle permits fine control of the rate of fringe displacement without the use of a needle valve. For air, a displacement of about 60 fringes is obtained for a 6-cm cell; reasonable accuracy for the refractive indices of gases can be attaihed.

EXPERIMENT 6: Determining Thickness of Thin Transparent Films of Organic or Inorganic Materials.

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A method of determining the thickness of such films is outlined here. This method will serve to determine: (1) Refractive index, if thickness is known; and (2) Thickness, if refractive index is known.

#### Procedure:

I. Set up the Interferometer as shown below. First the instrument is adjusted to show white light fringes in left half of the field and showing the black band (see Fig. I next page).



2. Set up a telescope for viewing the bands. The reticule used in the ocular should be ruled so that there are about 20 divisions to either side of center. The micrometer screw is used to bring the center of the black band to the center line of the reticule. Fig. I shows this condition minus the image of the reticule. Substituted, in the drawing, for the center line of the reticule is the symbol,  $\triangleright$ .

3. If now the film to be measured is placed somewhere in optical path %1 of the instrument and positioned so as to appear in part of the white fringe area as shown in Fig. II, it will be noticed that the white light fringes have disappeared in the portion of light path that now passes through the film. This is due to the fact that the film has caused the optical path %1 to appear longer due to the refractive index of the film. To return the black band so it shows in the file, the optical path %2 must be lengthened. 4. The micrometer screw is slowly turned toward higher readings so that the carriage moves farther from the beam splitter.

While this is done a careful count must be made of the Hg light fringes, one by one, as they pass any given fixed position until the black band is visible through the film and in its original horizontal position as in Fig. III



5. To determine the thickness, the formula given in Experiment 5 is used as follows:

$$t = \frac{\lambda_{air} \Delta^{n}}{2(\mu - 1)}$$

where

t = Thickness  $\Delta n$  = Number of fringes passed over  $\mu$  = Index of refraction of the film material  $\lambda_{air}$  = Wave length of Hg light = 5460Å For example, suppose  $\triangle n = 10$ ,  $\mu = 1.5$ , then

$$t = 10 \times 5460 = 54,600 \text{ Å} = 5.46 \text{ micron} = .00546 \text{ mm}.$$
  
2 x .5

6. In measurement of very thin films where the displacement is less than one fringe (see Fig. V) measure as follows:

 $D_1 = 1/4D_2$ 

and  $D_2$  corresponds to 1/2 wave length path difference ( $\Delta n = 1/2$ ). Therefore

$$\Delta n = 1/4 \times 1/2 = 1/8$$

Again, assuming  $\mu = 1.5$ , the thickness is given as before by

$$t = \frac{1/8 \times 5460}{2 \times .5} = 582 \text{ Å}$$

# EXPERIMENT 7: Determination of Wave Length Differences for the Balmer Lines of Hydrogen and Deuterium.

<u>Procedure</u>: For this experiment a Heavy Water Balmer Tube light source is used with the M-4 Interferometer. A Number 16 Wratten filter or equivalent is necessary for observation of the red Balmer lines, and a Number 45 Wratten filter or equivalent is necessary for observation of the blue Balmer lines without interference from the other lines of the Balmer series. A cylindrical lens of about 2.5 inches focal length (or about 15 diopters) placed approximately 2 inches from the Balmer tube is helpful in providing more uniform illumination to the field viewed in the interferometer. A diffuser plate (ground glass or waxed paper) and the appropriate filter are located between the cylindrical lens and the interferometer.

With the Number 15 Wratten filter or equivalent in place, obtain a good pattern of fringes. The wavelength of the red Balmer line may be determined using the procedure of Experiment 1.

Loosen the carriage lock screw. Now, with the bull's eye in view, place a thumb on each side of the interferometer base, and index and middle fingers on each side of the carriage. <u>Very</u> gently push the carriage until the bull's eye disappears. Place a centimeter scale on top of the beam splitter and the compensator. Measure the distance between the index marks in the top center of the beam splitter and compensator frames. Estimate distances to 0.1 millimeters. Again gently push the carriage. The bull's eye will reappear and then again disappear. Measure the distance between index marks. Repeat this procedure for five to ten successive disappearances of the bull's eye. In reducing the data only the initial and final measurements are used. However, a reasonable uniformity of the differences between intermediate measurements ensures that a disappearance of the bull's eye has not been missed in moving the interferometer carriage.

Between successive disappearances of the bull's eye, we have moved the carriage one more wavelength for the shorter wavelength line than for the longer wave length line.

$$2(d_2 - d_1) = \lambda_1 \Delta n = \lambda_2 (\Delta n + 1)$$

Where  $(d_2-d_1)$  is the distance the carriage is moved between successive disappearances of the bull's eye. However,

$$\lambda_1 = \lambda_2 + \Delta \lambda.$$
 Thus, 
$$\lambda_2 = \Delta n \Delta \lambda$$

$$2(d_2 - d_1) = \frac{\lambda_2 \lambda_1}{\sqrt{\lambda_1}}$$

Since  $\lambda_1$  is approximately equal to  $\lambda_2,$  we have:

$$\Delta \lambda = \frac{\lambda^2}{2(d_2 - d_1)}$$

An example of data taken and its reduction is given below.

$$\lambda = \frac{2(d_2 - d_1)}{\Delta n} = \frac{4 \times 10^{-5} (D_2 - D_1)}{\Delta n} = \frac{4 \times 10^{-3} (17.23 - 12.28)}{300} = 6.6 \times 10^{-5} \text{ cm}.$$

Disappearance	Distance between	Distance Between	
<u>of Bull's Eve</u>	Index Marks (cm)	Disappearances	
0	7.85		
ł	7.96	0.11	
2	8.08	0.12	
3	8.20	0.12	
4	8.32	0.12	
5	8.45	0.13	
6	8.57	0.12	
7	8.69	0.12	
8	8.80	0.11	
9	8.92	0.12	

$$d_2 - d_1 = \frac{1.07}{9} = 0.119$$
  
$$\Delta \lambda = \frac{\lambda^2}{2(d_2 - d_1)} = \frac{(6.6 \times 10^{-5})^2}{0.238} = 1.83 \times 10^{-8} \text{ cm}.$$

More accurate values for the red lines are:

 $\lambda$  = 6563 Angstrom Units for Ha and  $\Delta\!\lambda$  = 1.79 Angstrom Units.

With the Number 45 Wratten filter or equivalent in place, the experiment may be performed for the blue Balmer line. An example of data taken and its reduction is given below.

$\lambda = 2(d_2 - d_1) = 4 \times 10^{-5}$	$(D_2 - D_1) = 4 \times 10^{-5}$	$\frac{15.53-11.90}{200} = 4.9 \times 10^{-5} \text{ cm}.$
∆n ∆n		500
Disappearance	Distance between	Distance Between
of bull's eve	<u>Index Marks (cm)</u>	Disapoearances
0	5.03	
l	8.13	0.10
2	3.22	0.09
3	8.31	0.09
4	ê.40	0.09 .
5	<b>3.</b> 49	0.09

$$\Delta \lambda = \frac{\lambda^2}{2(d_2 - d_1)} = \frac{(4.9 \times 10^{-5})^2}{0.184} = 1.31 \times 10^{-8} \text{ cm}.$$

More accurate values for the blue lines are:

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;

 $\lambda$  = 4861 Angstrom Units for HB and  $\Delta \lambda$  = 1.33 Angstrom Units.

<u>Discussion</u>: According to the Bohr theory, the wavelength of a spectrum line can be expressed by the formula:

$$\frac{1}{\lambda} = \frac{2\pi^2 m e^4 z^2}{c n^3} \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

Where  $\lambda$  is wavelength m is the mass of the electron e is the charge of the electron Z is the charge of the atomic nucleus c is the velocity of light h is Planck's constant n<sub>1</sub> is the quantum number of the initial state n<sub>2</sub> is the quantum number of the final state.

The Rydberg constant R =  $2\pi^2 me^4/ch^3$  so that

$$\frac{1}{\lambda} = RZ^2 \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right).$$

However, the electron does not rotate about a stationary nucleus but instead, both the electron and the nucleus rotate about the center of mass of the system. Thus the mass of the electron m should be replaced by the reduced

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mass  $\underline{Ma}$  where M is the mass of the nucleus. I +  $\underline{m}_{M}$ 

For the nucleus of hydrogen M = 1837 m and for the nucleus of deuterium M = 3674 m. Thus the Rydberg constant is slightly different for deuterium than for hydrogen. For hydrogen R = 109677.759. For deuterium R = 109707.387. For a nucleus of infinite mass R = 109737.424.

In the Bohr theory formula above Z = 1 for hydrogen and deuterium. For the Balmer series  $n_1 = 2$ . The red line  $H_{\alpha}$  corresponds to  $n_2 = 3$  and the blue line  $H_{\beta}$  corresponds to  $n_2 = 4$ .

References:

H. E. White, Introduction to Atomic Spectra, McGraw-Hill, 1934, pp. 27-38.

G. Herzberg, Atomic Spectra and Atomic Structure, Dover 1944, pp. 19-26, 182-183.