

**Recitation 2**  
**2016-08-30**

**Exercise 0.7 from Sipser page 26**

**Exercise 0.8 from Sipser**

**Exercise 3**

Let  $R \subseteq A \times A$  be a binary relation as defined below. In which cases is  $R$  a partial order? a total order?

1.  $A =$  the strictly positive integers;  $aRb$  iff  $b$  is divisible by  $a$ .
2.  $A = \mathbb{N} \times \mathbb{N}$ ;  $(a, b)R(c, d)$  iff  $a \leq c$  or  $b \leq d$ .
3.  $A = \mathbb{N}$ ;  $aRb$  iff  $b = a$  or  $b = a + 1$ .
4.  $A$  is the set of all English words;  $aRb$  iff  $a$  is strictly shorter than  $b$ .
5.  $A$  is the set of all English words;  $aRb$  iff  $a$  is the same as  $b$  or  $a$  occurs more frequently than  $b$  in Sipser's book.

**Exercise 4**

Let  $R_1$  and  $R_2$  be any two partial orders on the same set  $A$ . Show that  $R_1 \cap R_2$  is a partial order.

**Exercise 5**

Let  $A$  be any set, let  $\mathbb{B}$  be the set of booleans. We write  $A \rightarrow \mathbb{B}$  for the set of all functions from  $A$  to  $\mathbb{B}$ . Prove that there exists a bijection between  $A \rightarrow \mathbb{B}$  and the powerset of  $A$ ,  $\mathcal{P}(A)$ .